











Logistic Regression (4)

• Linear classification uses hard threshold

$$h(x) = sign(\partial^T x)$$

• Linear regression uses no threshold

$$h(x) = \partial^T x$$

- In logistic regression, a compromise of both models is made such that it restricts the output to the probability range [0, 1]
- This is done through the following model

$$h(x) = Q(\mathcal{A}^T x)$$





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Logistic Regression (7)

- The logistic function is a link function that is best suited for the binomial distribution
- The parameters are chosen to maximise the liklehood of observing the sample values rather than minimizing the sum of squared errors (like in ordinary regression)

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Logistic Regression (8)

- Linear classification deals with binary events but the difference is that logistic regression is allowed to be uncertain with intermediate values between 0 and 1 reflecting this uncertainty
- Logistic regression function is known as soft threshold
- It is also called the sigmoid function

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Logistic Regression (9)

- It is widely used for classification problems
- No linear relationship required (as it applies a nonlinear log transformation to the predicted odds ratio)
- Required a large sample size (Max likelihood estimates are less powerful with small sample size)

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Hypothesis Representation

- The hypothesis representation, which is the function that we will use to represent a hypothesis when we have a classification problem
- Using a simple linear regression to approach a classification problem has the problem that predicting y might get larger than 1 or smaller than zero (given a value of x)







$$h(x) = p(y=1 \mid x; \alpha)$$





























